# Hodge's Conjecture Clay Institute Millenium Problem Solution 

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#### Abstract

Here is a paper that provides a proof for the Hodges Conjecture that all solutions to the complex Manifold are linear. A simple way to understand this is the Ln function.


## 1. Introduction

## Statement of the Hodge Conjecture

Let
$\operatorname{Hdg}^{k}(X)=H^{2 k}(X, \mathbf{Q}) \cap H^{k, k}(X)$.
We call this the group of Hodge classes of degree $2 k$ on $X$.
The modern statement of the Hodge conjecture is:
Hodge conjecture. Let $X$ be a non-singular complex projective manifold. Then every Hodge class on $X$ is a linear combination with rational coefficients of the cohomology classes of complex subvarieties of $X$.
A projective complex manifold is a complex manifold which can be embedded in complex projective space. Because projective space carries a Kähler metric, the Fubini-Study metric, such a manifold is always a Kähler manifold. By Chow's theorem, a projective complex manifold is also a smooth projective algebraic variety, that is, it is the zero set of a collection of homogeneous polynomials.

## 2. Modelling the Complex Manifold



## ILLUSTRATION 1 RAILROAD TRACKS

Two parallel lines when viewed from above are 0 degrees difference in slope. When the same lines are viewed in perspective, the angle between them is less than 90 degrees ( $\mathrm{Pi} / 2$ ). These appear to go to infinity whereas we know they don't. From the illustration on the right. This phenome can be modelled by a box within a circle. In fact, this circle is just one particular case, but the analogy can be used to model any vector space that is complete.


ILLUSTRATION 2 CIRCLE PROPERTIES
We know from simple trigonometry that,
Sin theta $=y / R \quad y=R$ sin theta
Cos theta $\mathrm{x} / \mathrm{R} \quad \mathrm{x}=\mathrm{R} \cos$ theta
The equation of a circle is, $x^{\wedge} 2+y^{\wedge} 2=r^{\wedge} 2$
Inserting,
$\mathrm{R}^{\wedge} 2 * \cos ^{\wedge} 2$ theta $+\mathrm{R}^{\wedge} 2 \sin \wedge 2$ theta $=\mathrm{R}^{\wedge} 2$
Let $\mathrm{R}=1$ (arbitrary)
$\operatorname{Cos}^{\wedge} 2$ theta $+=\sin ^{\wedge} 2$ theta $=1$
Cos theta $+\sin$ theta $=$ sqrt $1=+/-1$
Cos dtheta/dt=sin dtheta/dt=+/-1
W=dtheta/dt $n$
Cos $\mathrm{w}+\sin \mathrm{w}=1$
Now Area of a circle $=\operatorname{Pi} \mathrm{R}^{\wedge} 2=\mathrm{Pi}(1)^{\wedge} 2=\mathrm{Pi}$
Cos $\mathrm{w}+\sin \mathrm{w}=\mathrm{R}^{\wedge} 2$
Cos $\mathrm{w}+\sin \mathrm{w}=\mathrm{A} / \mathrm{Pi}$
Consider the Area of the square x by y
A $s q=x y$
Asq' $=(x y)^{\prime}$
$=\{$ Rsin theta $)($ Rcos theta $)$,
$=R^{\wedge} 2 \sin$ theta $\cos$ theta]
$=2 R(-\cos$ theta $\sin$ theta $]$
Integral Asq' $=\mathrm{A}-2 \mathrm{R}^{\wedge} 2 / 2 \sin$ theta $(-\cos$ theta)
Set Asq=0
$0=R^{\wedge} 2 \sin$ heta cos theta
Sin theat $=0 \quad$ or $\cos$ theta $=0$
Theta $=\{0,90,180,270,360\}$
Cos $\mathrm{w}+\sin \mathrm{w}=\mathrm{A} / \mathrm{t}$
Integral $w=$ Integral dTheta/dt
$W^{\wedge} 2 / 2=$ theta
$\operatorname{Cos}\left(w^{\wedge} 2 / 2\right)+\sin \left(w^{\wedge} 2 / 2\right)=\mathrm{A} / \mathrm{Pi}=0 / \mathrm{Pi}=0$
$\mathrm{W}^{\wedge} 2 / 2=\{0,90,180,270,360\}$
$\mathrm{W}=\{0, \mathrm{Pi}$, sqrt $\mathrm{Pi}, \operatorname{sqrt}(2 \mathrm{Pi})$, sqrt $3 \mathrm{Pi} / 2)\}$
$W=\{0,1.7725,2.5066,2.1708\}$ rads
Substituting each of these in to the above equation:
$\mathrm{X} \cos \mathrm{w}+\sin \mathrm{w}=0$
$\operatorname{Cos} 0+\sin 0($ not $=) 0$
$\operatorname{Cos}($ sqrt Pi) $)+\sin ($ sqrt Pi) $($ not $=0$
$\operatorname{Cos}(\operatorname{sqrt}(2 \mathrm{Pi})+\sin (\operatorname{sqrt}(2 \mathrm{Pi})($ not $=) 0$
$\operatorname{Cos}(3 \mathrm{Pi} / 2)+\sin (\operatorname{sqrt} 3 \mathrm{Pi} / 2)=($ not $=) 0$
All these conditions fail.
Now, the Area of the square $=x y$
Asq=xy
Asq=[Rsin theta][Rcos theta]
$=A r e a / R=P i R$
Let $\mathrm{R}=1$
$\mathrm{Pi}=\sin$ theta $* \cos$ theta

## Derivative:

$\mathrm{C} 1=(\cos$ theta)(-in theta)
$\mathrm{C} 1=-\mathrm{Pi}$

## Derivative:

C2 $=(-\sin$ theta $)(-\cos$ theta)
$\mathrm{C} 2=\sin$ theta $\cos$ theta
$-\mathrm{c} 1=\mathrm{c} 2=-\mathrm{Pi}$
$\mathrm{C} 1=\mathrm{Pi}$
$\mathrm{C} 2=-\mathrm{Pi}$
$-\mathrm{c} 1=\sin$ theta $\cos$ theta
$\mathrm{C} 2=\sin$ theta cos theta
$-\mathrm{C} 1==\mathrm{C} 2$
$-\mathrm{Pi}=-\mathrm{Pi}$
True!
Asq=xy
$0=$ Rsin theta cos theta
Sin theta=0
Theta=0, Pi, 2Pi
Cos theta=0
Theta $=\mathrm{Pi} / 2,3 \mathrm{Pi} / 2$
Theta $=\{0, \mathrm{Pi} / 2, \mathrm{Pi}, 3 \mathrm{Pi} / 2,2 \mathrm{Pi}\}$
Theta $=\{ ) \mathrm{Pi} / 2,1 \mathrm{Pi} / 2,2 \mathrm{Pi} / 2,3 \mathrm{Pi} / 2,4 \mathrm{Pi} / 2\}$
Theta=nPi/2
$\mathrm{n}=0,1,2,3,4 \rightarrow$ Asq=0 (Linear Set $\}$
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3. Two Parallel Vectors such Rail Road Tracks have a difference between their Direction of Zero.


ILLUSTRATION 3 LINEAR SET n AND THE DERIVATIVE
Asq' $=0=\mathrm{Cl}$
Asq=xy
Asq=Rsin theta cos theta
Asq ${ }^{\prime}=\mathrm{C} 1=\left[\mathrm{R}^{\wedge} 2 \sin \text { theta cos theta }\right\}^{\prime}$
$-2 R(\cos$ theta sin theta
$0=C 1=-2 R \cos$ theta sin theta
Derivative:
$0=\cos$ theta $\sin$ theta
Cos theta $=0$
Sin theta-=0
Theta $=\{n P i / 2) n==? 0,1,2,3,4$ (Linear zSet$)$
Linear Set=[Linear Set $\}^{\prime}$
nPi/2=L.S.
$n P i / 2=0$
$\mathrm{n}=0$
$\mathrm{n}=\{$ Null Set $\}$
Arsq=xy
$=R \sin$ theta $\cos R \cos$ theta
Sin $0 \cos 0=$
$=(01)(1)$
$=0$
Asq=0
So if the derivative and Integral of the Linear Set are equal:
$Y=y$ '
Integral $\mathrm{y}=\mathrm{y}$ '
$Y^{\wedge} 2 / 2=y$
$Y^{\wedge} 2 / 2-y=0$
$\mathrm{Y}(\mathrm{y}-2)=0$
$\mathrm{Y}=0, \mathrm{y}=2$
$Y=y^{\prime}=y^{\prime \prime}$,
Asq $=\mathrm{e}^{\wedge} \mathrm{x}$
$Y=2=e^{\wedge} x$
$Y=\operatorname{Ln} 2=x$
$\mathrm{X}=0.6931$
$\mathrm{Y}=\mathrm{x}$
$\mathrm{Y}=\mathrm{mx}+\mathrm{b}$
$\mathrm{Y}=(1) \mathrm{x}=0$
$\mathrm{Y}=\mathrm{x}$ (Linear)
$Y=e^{\wedge} x$
$\mathrm{Y}^{\prime}=\mathrm{e}^{\wedge} \mathrm{x}=0$
X=-Infinity
TWO PARELL VECTOR CAN HAVE APPEAR TO JOIN AT INFINITY.
Now,
$\operatorname{Ln}(0)=1 / .0$
$\mathrm{E}^{\wedge}(\operatorname{Ln} 0)=0=\mathrm{e}^{\wedge} 196$
$0=1.3235 x$ 10^85
$1 / \mathrm{x}=196$ (Infinity)
$\mathrm{X}=1 / 196=0.005102$
$\mathrm{x} / \mathrm{Pi}=0.05102=1624 \sim 1618=$ Golden Mean
$\mathrm{x}=1.618 \mathrm{Pi}$
$0.618 \mathrm{x}=\mathrm{x} / 1.618=\mathrm{Pi}$
Sqrt $(-1) \mathrm{x}=\mathrm{Pi}$
Sqrt(-1)(0)=Pi
$0=\mathrm{Pi} / 4$
Golden Mean
$\mathrm{X}^{\wedge} 2-\mathrm{x}-1=0$
$\mathrm{X}=1.618,0.618$
$\mathrm{X}^{\wedge} 2-\mathrm{x}-1=0$
(Ln 0)^2-Ln o-1=0
Uinfinity^2-Infinity-1=0
Derivative $=$ slope $=\mathrm{m}=$ LINEAR RELATIONSHIP BETWEEN x and y
$2 *$ Infinity- $1-1=0$
$2 *$ Inifinity $=2$ Infinity $=1$
$\operatorname{Ln}(0)=\mathrm{Ln}(\mathrm{Pi} / \mathrm{sqrt}(-1)=1.626 \rightarrow 1.618$
Ln (0)=-Infinity=1
So the difference in the parallel railroad tracks is 0 , When the angle is <90 they appear Infinite. And the solution to is linear.
4. GOLDEN MEAN EQUATION: where the Multiple Meets the Fraction I.E., at the NUMBER 1
$X^{\wedge} 2-x-1=n^{\wedge} 2 / 2$
THE RATE OF CHANGE OF THE APPROACH TO 1 IOF THE GOLDEN MEAN FUNCTION IS THE DERIVATIVE. SET THE DERIVATIVE =n OR THE LINEAR SET.

Derivative
$2 \mathrm{x}-1=\mathrm{n}$
$2 \mathrm{x}-1=0$
$X=1 / 2$
$2 \mathrm{x}-1=1$
$\mathrm{X}=1$
$2 \mathrm{x}-1=2$
$X=3 / 2$
$2 \mathrm{x}-1=3$
$X=4 / 2=2$
Area of a circle $=\mathrm{PiR}^{\wedge} 2$
$\mathrm{R}=1$
Area=Pi
Pi* $0=0$
Pi* $1 / 2=\mathrm{Pi} / 2$
Pi* $1=\mathrm{Pi}$
$\mathrm{Pi} * 3 / 2=3 \mathrm{Pi} / 2$
Pi* 2
$=2 \mathrm{Pi}$
Derivative of Golden Mean $=\{0, \mathrm{Pi} / 2, \mathrm{Pi}, 3 \mathrm{Pi} / 2,2 \mathrm{Pi}\}$
$=$ Theta for $\mathrm{n} \rightarrow 0,1,2,3,4$
5. Ln Function


## ILLUSTRATION 4 LN FUNCTION

The universal function is when $y=y^{\prime}=y^{\prime}$ '. So, since we are sitting at 1 , the solution is linear when the angle between the two vectors is zero. We move toward 0 , the angle between the two vectors goes to infinity.

## 6. CONCLUSION

So, this proves that the solution is linear and infinite at the same time. The diagonal of every box has a $\sin$ and a cosine component. So, this proves that every box has the same solution: Linear and Infinite and zero at the same time.

## References

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