

Quantization of Gravitational Wave by Klein-Gordon Equation

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Abstract: In the general relativity theory, we find gravitational matter wave by Klein-Gordon wave equation. Specially, this article is that Quantization of gravitational wave is made by Klein-Gordon wave equation. We assume this matter wave as Dark Matter.

Keywords: General relativity theory, Gravitational Wave; Klein-Gordon wave equation; Gravitational matter wave; Dark matter

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1. INTRODUCTION

In the general relativity theory, our article's aim is that we find the quantization of gravitational wave by Klein-Gordon wave equation.

At first, gravitational wave equation is

$$(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2})h_{\mu\nu} = 0 \quad (1)$$

The solution, gravitational wave function $h_{\mu\nu}(x)$ is

$$h_{\mu\nu}(x) = a_{\mu\nu} \exp(ik_\lambda x^\lambda) + a_{\mu\nu}^* \exp(-ik_\lambda x^\lambda) \quad (2)$$

In this time,

$$k_\lambda k^\lambda = -\frac{\omega_0^2}{c^2} + k_0^2 = 0, \quad k_\lambda = (\frac{\omega_0}{c}, \vec{k}_0), \quad k^\lambda = (-\frac{\omega_0}{c}, \vec{k}_0) \quad (3)$$

The constant tensor $a_{\mu\nu}$ is the polarization tensor.

$$a_{\mu\nu} = a_{\nu\mu} \quad (4)$$

Harmonic coordinate condition is

$$(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2})\epsilon_\nu = \frac{\partial h_{\nu}^{\mu}}{\partial x^{\mu}} - \frac{1}{2} \frac{\partial h^{\mu}}{\partial x^{\nu}} \quad (5)$$

$$k_{\mu} a^{\mu}_{\nu} = \frac{1}{2} k_{\nu} a^{\mu}_{\mu} \quad (6)$$

The coordinate transformation is

$$x'^{\mu} = x^{\mu} + i\epsilon^{\mu} \exp(ik_{\lambda} x^{\lambda}) - i\epsilon^{*\mu} \exp(-ik_{\lambda} x^{\lambda}) \quad (7)$$

According to Eq(7), the transformation of the polarization tensor is

$$a'_{\mu\nu} = a_{\mu\nu} + k_{\mu}\epsilon_{\nu} + k_{\nu}\epsilon_{\mu} \quad (8)$$

2. QUANTIZATION OF GRAVITATIONAL WAVE BY KLEIN-GORDON EQUATION

The speed of Gravitational wave is light speed. If we make matter by Gravitational space-time, this matter moves as the usual matter. We consider the matter interacting only gravity. Hence, we assume this matter as Dark Matter.

At first, gravitational matter wave equation is

$$(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2})h_{\mu\nu} = \frac{m_0^2 c^2}{\hbar^2} h_{\mu\nu} \quad (9)$$

The solution, gravitational matter wave function $h_{\mu\nu}(x)$ is

$$h_{\mu\nu}(x) = a_{\mu\nu} \exp(ik_{\lambda}x^{\lambda}) + a_{\mu\nu}^* \exp(-ik_{\lambda}x^{\lambda}) \quad (10)$$

In this time,

$$-k_{\lambda}k^{\lambda} = \frac{\omega_0^2}{c^2} - k_0^2 = \frac{m_0^2 c^2}{\hbar^2}, \quad E = \hbar\omega_0, \quad \vec{P} = \hbar\vec{k}_0, \quad (11)$$

$$k_{\lambda} = (\frac{\omega_0}{c}, \vec{k}_0), \quad k^{\lambda} = (-\frac{\omega_0}{c}, \vec{k}_0)$$

The constant tensor $a_{\mu\nu}$ is the polarization tensor.

$$a_{\mu\nu} = a_{\nu\mu} \quad (12)$$

Harmonic coordinate condition is in gravitational matter wave by Eq(5),Eq(6)

$$k_{\mu}a^{\mu}_{\nu} - \frac{1}{2}k_{\nu}a^{\mu}_{\mu} = \frac{m_0^2 c^2}{\hbar^2} \epsilon_{\nu} = (\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2})\epsilon_{\nu} \quad (13)$$

3. CONCLUSION

We find the gravitational matter wave by Klein-Gordon wave equation. We find the quantization of gravitational wave by Klein-Gordon wave equation.

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